(see Bowen & Tanmer, High Resolution X-ray Difffractometry and Topography, Chap. 3)



mismatch

(a)









## Common epilayer defects

(see Bowen & Tanner, High Resolution X-ray Diffractometry and Topography, Chap. 3)

## Common epilayer defects

# Investigate using rocking curves











<sup>(</sup>g)

inhomogeneity











inhomogeneity

# Investigate using rocking curves

## Film thickness

Integrated intensity changes increases w/ thickness Interference fringes

## Mismatch



relaxed



Mismatch

Layer & substrate peaks split - rotation invariant

Measure, say, (004) peak separation  $\delta \theta$ , from which

 $\delta d/d = -\delta \theta \cot \theta = m^*$  (mismatch)



Misorientation

First, determine orientation of substrate

rotate  $\phi$  to bring plane normal into counter plane

do  $\omega$  scans at this position and at  $\phi$  + 180°

orientation angle = 1/2 difference in two angles



Misorientation

First, determine orientation of substrate

Layer tilt (assume small)

layer peak shifts w//  $\phi$  in  $\omega$  scans



Misorientation

First, determine orientation of substrate

Layer tilt (assume small)

layer peak shifts w/  $\phi$  in  $\omega$  scans



Misorientation

First, determine orientation of substrate

Layer tilt (assume small)

layer peak shifts w/  $\phi$  in  $\omega$  scans



Misorientation

First, determine orientation of substrate

Layer tilt (assume small)

layer peak shifts w/  $\phi$  in  $\omega$  scans

make 3 shift measurements  $(\Delta_0, \Delta_{90}, \Delta_{180})$ then  $\Delta_0 = \beta \cos \omega$   $\Delta_{90} = \beta \cos (\omega + 90)$   $\Delta_{180} = \beta \cos (\omega + 180)$  $\Delta_{90}/\Delta_0 = \tan \omega$ 



**Dislocations** 

From:

high mismatch strain, locally relaxed local plastic deformation due to strain growth dislocations

**Dislocations** 

From:

high mismatch strain, locally relaxed local plastic deformation due to strain growth dislocations

Estimate dislocation density  $\rho$  from broadening  $\beta$  (radians) & Burgers vector b (cm):

 $\rho = \beta^2 / 9 b^2$ 

## Curvature

R = radius of curvature, s = beam diameter

angular broadening = s/R =  $\delta \theta$ 

beam	radius	broadening
5 mm	100 m	10"



Relaxation

Need to measure misfit parallel to interface

Both mismatch & misorientation change on relaxation



Interplanar spacings change with mismatch distortion & relaxation – changes splittings

Relaxation

Need to measure misfit parallel to interface

Both mismatch & misorientation change on relaxation



So, also need misfit perpendicular to interface

Then, % relaxation is

$$R = \frac{a_1 - a_s}{a_1^R - a_s} \times 100$$

Relaxation

Grazing incidence

Incidence angle usually very low....~1-2°

Limits penetration of specimen



Relaxation

Grazing incidence

Incidence angle usually very low....~1-2°

Limits penetration of specimen

Penetration depth - G(x) = fraction of total diffracted intensity from layer x cm thick compared to infinitely thick specimen

 $G(x) = 1 - \exp\left(\frac{-2\mu\rho x}{\sin\theta}\right) = \frac{\text{intensity from a layer x cm thick}}{\text{intensity from an infinitely thick sample}}$ 





Penetration depth - G(x) = fraction of total diffracted intensity from layer x cm thick compared to infinitely thick specimen

$$G(x) = 1 - \exp\left(\frac{-2\mu\rho x}{\sin\theta}\right) = \frac{\text{intensity from a layer x cm thick}}{\text{intensity from an infinitely thick sample}}$$

Relaxation

Grazing incidence

Incidence angle usually very low....~1-2°

Reflection not from planes parallel to specimen surface



Relaxation

Grazing incidence

If incidence angle ~0.1-5° & intensity measured in symmetric geometry (incident angle = reflected angle),, get reflectivity curve



Relaxation

Need to measure misfit parallel to interface

Use grazing incidence e.g., (224) or (113)



## Relaxation

Use grazing incidence e.g., (224) or (113)

Need to separate tilt from true splitting

Tilt effect reversed on rotation of  $\phi = 180^{\circ}$ 

Mismatch splitting unchanged on rotation



## Relaxation

Use grazing incidence e.g, (224) or (113)

For grazing incidence:

 $\Delta \Theta_{i} = \delta \Theta + \delta \phi$ 

 $\delta \theta = \theta$  splitting betwn substrate & layer



## Relaxation

Use grazing incidence e.g, (224) or (113)

For grazing incidence:

 $\Delta \theta_{\rm ij} = \delta \theta + \delta \phi$ 

 $\Delta \theta_{\rm e} = \delta \theta - \delta \phi$ 

Can thus get both  $\delta \theta$  and  $\delta \phi$ 



#### Relaxation

Also,





$$\frac{4\sin^2\theta_{l}}{\lambda^2} = \frac{h^2 + k^2}{a_{l}^2} + \frac{l^2}{c_{l}^2}$$

$$\sec^2 \phi_i = \frac{c_i^2}{l^2} \left\{ \frac{h^2 + k^2}{a_i^2} + \frac{l^2}{c_i^2} \right\}$$

## Relaxation

# Also,

$$\theta_l = \theta_s + \delta\theta$$
$$\phi_l = \phi_s + \delta\phi$$

## And

$$\frac{4\sin^2\theta_i}{\lambda^2} = \frac{h^2 + k^2}{a_i^2} + \frac{l^2}{c_i^2} \qquad \qquad \sec^2\phi_i = \frac{c_i^2}{l^2} \left\{ \frac{h^2 + k^2}{a_i^2} + \frac{l^2}{c_i^2} \right\}$$

## Finally

$$c_{l} = \frac{l\lambda}{2\sin\theta_{l}\cos\phi_{l}} \qquad a_{l} = \frac{l\lambda}{2\sin\theta_{l}}\sqrt{\frac{h^{2}+k^{2}}{l^{2}}}$$

$$R = \frac{a_l - a_s}{a_l^R - a_s} \times 100$$

Homogeneity

Measure any significant parameter over a grid on specimen

**Ex: compositional variation** 

get composition using Vegards law measure lattice parameter(s) – calculate relaxed mismatch



## Homogeneity

#### Measure any significant parameter over a grid on specimen

Ex: variation of In content in InAIAs layer on GaAs



Thickness

For simple structure layer, layer peak integrated intensity increases monotonically w/ thickness



Specimen angle (arc seconds)

calculated curves

Thickness

For simple structure layer, layer peak integrated intensity increases monotonically w/ thickness

Note thickness fringes

Can use to estimate thickness



Specimen angle (arc seconds)

calculated curves



Thickness

For simple structure layer, layer peak integrated intensity increases monotonically w/ thickness



Specimen angle (arc seconds)

calculated curves